# Introduction

For this assignment, using a 3D MRI brain image data (*sub-13\_T1w.nii.gz*), we implement tissue labeling using two approaches:

* First use one of the background removal approaches (binary classifiers such as ISODATA, Otsu, or Bayesian) discussed in the class as pre-processing step to identify foreground from background pixels and then classify foreground pixels into white matter, gray matter, csf, and no-brain tissue (Ex. scalp).
* Or use the approach discussed in the module to directly divide pixels into background, white matter, gray matter, csf, and no-brain tissue (Ex. scalp).
* Implementations should include gain factor estimation.

We need to display the original slice along all different tissues and gain factor images. And we limit the gain factor estimation display only to the brain area.

# Main Work

1. We upload the NIFTI image **sub-13\_T1w.nii.gz** from the folder data. Make sure that the folder exists with the file. If not, please modify the line: *vol = niftiread('data/sub-13\_T1w.nii.gz')* to point to the location with the file.
2. The image is flipped to facilitate image manipulation.
3. Then we look at the histogram intensity of slice 143 which shows that it is bimodal so the OTSU’s method should be the most appropriate to distinguish background from foreground pixels.

A graph of a person

Description automatically generated

We also compute the classification threshold with Bayesian Minimum Error Thresholding algorithm. If we compare the classification of foreground pixels from background pixels**:**

* The resulting binary mask from Otsu’s method, appears to segment the brain well, but it includes some background artifacts and fails to exclude portions of the scalp completely.
* Minimum Error Thresholding’s threshold (T = 0.51) is higher than Otsu's threshold (T=0.18), leading to a more aggressive exclusion of background pixels.
* The binary mask from Minimum Error Thresholding, is cleaner and includes fewer background artifacts, but it potentially excludes some brain tissues near the edges, such as regions close to the scalp or the outer parts of the brain.

To effectively identify not only white and gray matter but also cerebrospinal fluid (CSF) and non-brain tissue (e.g., scalp), the preprocessed image generated using Otsu’s method is preferred due to its ability to retain more detailed segmentation. In addition, the absolute "goodness" coefficient—a measure of thresholding effectiveness—is significantly higher for Otsu’s method (0.8) compared to the minimal value for the "minimum error thresholding" method (0.09) (**Fig. 1**).

A close-up of a brain scan

Description automatically generated

**Figure 1:** Automatic Thresholding using Otsu’s Method (middle) and Minimum Error Thresholding(right).

Otsu’s method is implemented through two key functions: **otsuThreshold** and **makeMeanTables**, which adhere to the steps outlined in **Algorithm 1**. These functions compute the optimal threshold by minimizing the intra-class variance, consistent with the original Otsu's algorithm.

Similarly, the **Minimum Error Thresholding** approach is implemented based on **Algorithm 2**. The corresponding functions, **minimumErrorThreshold** and **makeSigmaTable**, calculate the threshold by minimizing the probabilistic classification error between the foreground and background classes.

A screenshot of a paper

Description automatically generated

**Algorithm 1: Otsu’s Method.**

**A screenshot of a computer

Description automatically generated**

**Algorithm 2: Minimum Error Thresholding.**

**A screenshot of a math equation

Description automatically generated**

**MakeSigmaTable function.**

1. We perform tissue classification as described in [1] using only the foreground pixels obtained from the binarized image generated by Otsu's method. The implementation follows these steps:
2. **Initialization**:  
   Initial estimates for the centroids γk​ are obtained, and the gain field gj is initially set to 1 for all pixels.
3. **Indicator Function Update**:  
   The indicator function zj\*​ is solved by minimizing the energy function:

A black and white text

Description automatically generated with medium confidence

where yj​ is the intensity of pixel j, β controls the smoothness of the segmentation, Nj​ denotes the neighborhood of pixel j, and matrix V “ensures that a pixel belonging to the same class as its neighbors is favored over other configurations”:

V = [1,…,1]T [1,..,1] – I where I is identity matrix.

1. **Centroid Update**:  
   The means for each tissue class are updated using the current indicator function zj and gain field gj.

A black and white rectangular object with letters and numbers

Description automatically generated

1. **Gain Field Update**:  
   The gain field is refined by solving the following equation for the polynomial coefficients fn:

A black text with a white background

Description automatically generated with medium confidence

A black text on a white background

Description automatically generated

A black and white symbol

Description automatically generated

where Pn(j) are the basis functions representing the gain field, and fn​ are the coefficients to be determined.

Code implemented in functions:

* initializeCentroids
* getNeighbors
* computePolynomialBasis
* estimateIndicatorFunctionWithGain\_ICM\_V
* updateCentroids
* unsupervisedClassification
* preprocessAndClassify

1. When displaying the original slice, segmented image, and gain field side by side (function **showResultsWithGain**), we observe the following (**Fig. 2**):

**1. Original Slice (Left Panel):**

* The original slice clearly displays anatomical structures but exhibits non-uniform intensity distribution due to field inhomogeneities or imaging artifacts.
* These inhomogeneities emphasize the importance of gain field correction to normalize intensities for accurate tissue classification.

**2. Tissue Segmentation (Middle Panel):**

* The segmentation distinguishes brain tissue from non-brain regions (e.g., background and scalp), leveraging Otsu's thresholding to identify foreground pixels.
* While effective, segmentation may suffer from artifacts or misclassifications at boundaries or regions with subtle intensity differences due to uncorrected inhomogeneities.

**3. Gain Field (Right Panel):**

* The gain field reflects multiplicative correction factors applied across the image to address intensity inhomogeneities.
* Bright areas indicate regions requiring higher intensity correction (e.g., edges where intensities were underestimated).
* Dark areas represent regions closer to true intensity values with minimal correction.
* The smooth, continuous gain field demonstrates successful bias correction, enabling more reliable tissue analysis.

A close-up of a brain

Description automatically generated

**Figure 2:** unsupervised tissue classification on preprocessed image using Otsu’s method with gain factor impact (right).

1. We now apply the same tissue classification but directly on the original image and observe:

The direct segmentation includes both brain and non-brain tissues, resulting in additional classes (e.g., scalp, background) being represented. Regions outside the brain, such as the periphery, are segmented into different classes: the segmentation seems less refined and more affected by intensity inhomogeneity, with more noticeable artifacts at the boundaries (Fig. 3).

**Key Differences:**

1. **Preprocessing with Otsu's Method**:

* Provides cleaner segmentation by isolating the brain region before classification.
* Gain field estimation focuses only on the relevant regions (brain tissue), leading to smoother corrections and less pronounced compared to direct classification gain.
* Algorithm convergence occurs quickly (after 3 iterations).

1. **Direct Classification**:

* Includes both brain and non-brain regions in the classification process, which increases the complexity of segmentation.
* Segmentation of tissue classes within the brain is less accurate due to interference from non-brain tissues.
* Gain field correction is less targeted and less smooth.

A close-up of a brain

Description automatically generated

**Figure 3:** unsupervised tissue classification on image itself (middle) with gain factor impact (right).

Functions:

* initializeCentroids
* getNeighbors
* computePolynomialBasis
* estimateIndicatorFunctionWithGain\_ICM\_V
* updateCentroids
* unsupervisedClassification
* classifyFullImage

# Challenges

* The unsupervised classification algorithm was challenging to implement just by reading the paper.

# Future Directions

* For comparison, an unsupervised tissue classification was implemented, and we observe that:
* The GMM approach yields a more detailed segmentation compared to direct classification or Otsu-preprocessed classifications using the previous models.
* Subtle intensity variations in white matter, gray matter, and cerebrospinal fluid (CSF) regions are captured more effectively.
* The classification appears to have fewer artifacts at tissue boundaries.
* The gain field appears smoother and more homogeneous than in previous approaches, indicating a better correction of intensity inhomogeneities across the brain.

The GMM-based gain field appears to provide a more refined correction across the brain tissue, particularly in regions with subtle intensity variations.

A close-up of a brain

Description automatically generated

**Figure 4:** unsupervised tissue classification using Gaussian Mixture Model on preprocessed image (middle) with gain factor impact (right).

**Limitations**:

* Some misclassifications are still present, particularly at the brain periphery (e.g., scalp regions classified as brain tissue).
* Sharp transitions in the segmentation are visible at some boundaries, indicating that GMM alone may still benefit from additional post-processing (e.g., spatial regularization).

The use of unsupervised tissue classification with GMM provides notable improvements in both segmentation accuracy and gain field estimation. By leveraging Gaussian mixture modeling, the approach captures intensity variations more effectively, leading to cleaner and more anatomically consistent tissue segmentation. While Otsu preprocessing combined with unsupervised classification relying on k-means provides a simpler pipeline, the GMM-based approach is more flexible and robust, especially for challenging regions. The authors [1] propose EM and fuzzy clustering approaches which may yield better tissue classification and worth investigating.

**Reference**

[1] Unsupervised tissue classification, DL Pham, PL Bazin, Handbook of Medical Image Processing and Analysis, 209-222

[2] Robust unsupervised tissue classification in mr image (2004), Dzung L. Pham et al. in Proceedings of the IEEE International Symposium on Biomedical Imaging

[3] Wilhem Burger – Mark J. Burge: Principles of Digital Image Processing - Advanced Methods - Springer